Constraining spatial pattern of early activity of comet 67P/C–G with 3D modeling of the MIRO observations

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ABSTRACT
Our aim is to investigate early activity (2014 July) of 67P/C–G with 3D coma and radiative transfer modeling of Microwave Instrument on the Rosetta Orbiter (MIRO) measurements, accounting for nucleus shape, illumination, and orientation of the comet. We investigate MIRO line shape information for spatial distribution of water activity on the nucleus during the onset of activity. During this period we show that MIRO line shape have enough information to clearly isolate contribution from ‘neck’ (Hapi) and bottom of large lobe (Imhotep), and compare it to the nominal case of activity from the entire illuminated surface. We also demonstrate that spectral line shapes differ from the 1D model for different viewing geometries and coma conditions relevant to this study. Specifically, line shapes are sensitive to the location of the terminator in the coma. At last, fitting the MIRO observations we show that the Imhotep region (possible distributed source of H2O sublimating from the icy grains in the coma lifted due to CO2 activities) contributes negligible fraction of the total number of water molecules into MIRO beam in the early activity. On the other hand, a strong enhancement of water activity from the ‘neck’ region seems required to fit the MIRO line shapes. This is consistent with earlier analysis of Rosetta results. Nevertheless, within the assumption of our coma and surface boundary conditions we cannot get a reasonable fit to all MIRO mapping observations in 2014 July. We provide discussion on how to enhance these results and resolve the found issues in the future.

Key words: comets: general – comets: individual: 67P/CG.

1 INTRODUCTION
The Microwave Instrument on the Rosetta Orbiter (MIRO) was designed to study the sub-surface heat transport as well as gas activity of the nucleus of 67P/Churyumov–Gerasimenko. Observations of MIRO began on 2014 May 24, and on June 6, the first water vapour spectral signature from 67P was detected at a heliocentric distance of 3.92 au (Gulkis et al. 2015), which was the second largest distance for water detection in a comet after Bockelée-Morvan et al. (2010). During the June–July time interval, Rosetta approached 67P going from a distance of 550 000 to 973 km, during which the field of view (FOV) of this single-pixel heterodyne spectrometer ranged from about 1200 to 2 km. Hence during this entire approach phase, the MIRO FOV remained larger than the effective radius of the nucleus of approximately 3.8 km for most of the time, providing an opportunity to study global water production rates. The MIRO observations during the 2014 June–July period are referred to here as the pre-rendezvous observations.

Gulkis et al. (2015) analysed early observations acquired by MIRO with a 1D radiative transfer model relying on the assumption of fully homogeneous semispherical nucleus (the Hesper model). The total H2O production rates were determined from the 557 GHz main isotope water line and monitored during the June–July period, which showed a periodical change related to nucleus rotation. Both, the significant blue shift of the spectral line and the time variations of the production rate indicated a preferential outgassing from the day side of the nucleus. The observations interpreted with the 1D model required a negligible activity from the unilluminated hemisphere, therefore, demonstrating a significant temperature contrast between the day and nightside as well as negligible contribution from distributed sources into un-illuminated regions.
The images acquired by the OSIRIS (Optical, Spectroscopic, and Infrared Remote Imaging System) during 2014 August–September lead to the first detailed characterization of the nucleus shape and yielded the digital shape model (Sierks et al. 2015). The nucleus of 67P is characterized by a small and a large lobe connected by a narrow ‘neck’ region. This information was used at later observations (August 2014) to suggest that the water outgassing is mainly localized in the neck region (Gulkis et al. 2015; Lee et al. 2015). Hässig et al. (2015) showed water densities at the location of S/C measured by the Rosetta Orbiter Spectrometer for Ion and Neutral Analysis (ROSETTA) when the comet was at 3.4 au from the Sun. They indicated the strongest activity to be correlated with Rosetta’s positions around the neck and north pole of the nucleus on the day side, and higher production rate in the ‘neck’ region could be one of the possible reasons. Lee et al. (2015) presented results indicating a noticeable spatial and diurnal variation of water outgassing on 67P based on MIRO observations when the spacecraft was already within 100 km from the nucleus in 2014 August. The authors pointed out that the largest water outgassing during this month occurred near the neck region, and outgassing activities in this region were found to be correlated with the local illumination condition, however, this was not the case for other regions.

MIRO observations during the spacecraft approach phase provided important information on the general mean outgassing, however, these results were limited, because the shape of 67P was not available when Rosetta first arrived at the comet. Hence, the detailed shape was not fully known and could not be taken into account during the first MIRO spectra interpretation. In this work we aim to extend the earlier studies of MIRO measurements from the pre-rendezvous stage, using the 3D nucleus shape model, appropriate illumination conditions on each facet and exact MIRO geometry. Our goal is to (1) constrain the water activity distribution on the nucleus using all the information in the MIRO measured line shape, (2) confirm or rule out possible distributed sources of water in the coma from the Imhotep region which showed a strong early activity in CO₂, and (3) take a first step forward from 1D idealizations used in current MIRO interpretations to begin to lead to the first detailed characterization of the nucleus shape and temperature, and the sub-millimetre band is further processed by the chirp transform spectrometer (Hartogh & Hartmann 1990) providing high spectral resolution for eight molecular transitions. The spectroscopic measurements are done in a frequency switched mode with a shift of ±5 MHz from the nominal frequency every 5 s during an integration time. This technique is used to minimize effects of baseline ripple and the possible short-term variations in gain drift (Gulkis et al. 2007a). The radiometric calibration is accomplished by (beam switching) observing hot and cold loads every 30 min to determine the gains of the two receivers.

2.2 MIRO observations: 2014 July

The MIRO instrument registered comet activity mainly from the 557 GHz ortho-H₂O transition in early 2014 June with estimated production rate Q[H₂O] ≈ 1 × 10²⁵ molecules s⁻¹ (Gulkis et al. 2015). At the time the heliocentric distance was about 3.95 au, well outside the water snow line. In fact all the unresolved nucleus observations, including the ones we aim to discuss in this paper happen at heliocentric distance larger than ~3.6 au. An incomplete log of pre-rendezvous observations made by MIRO are summarized in Table 1 including a flag indicating to which we applied our 3D model and with what degree of success (which will be discussed later in the paper).

3 MODELLING

The interpretation of MIRO observations requires a 3D radiative transfer model capable accounting for non-LTE effects in molecular excitation. The radiative transfer model requires 3D information on water molecules, temperature, and velocity distribution, along with spectroscopic parameters. In addition, we need a fast and reliable synthetic beam averaged spectra generator relying on the output populations of the 3D transfer code, along with precise MIRO pointing information.

We adopted the LIME package (Brinch & Hogerheijde 2010) (detailed later) for calculating the rotational populations of ortho-water in full 3D, and develop a routine to evaluate MIRO beam averaged radiance using precise pointing information from spice kernels (Acton 1996). These codes in turn require as an input a shape model (serving as a boundary condition), and also a coma characterized by water density, temperature, and expansion velocity covering the relevant computational domain.

3.1 The shape model

In this work we adopt nucleus shape model (SHAP?) (Preusker et al. 2017), but modified by Meshlab¹ to a resolution of 3000 facets. The average distance between two neighbouring vertices is 109.8 m and the average area of the facets for our shape model is 16 263 m². The low spatial resolution of the nucleus for the early observation is adequate since the projected MIRO beam size varies from more than 30 to about 2 km FWHM during this period. Our requirement is only to be able to clearly distinguish the main features of the shape, such as the Imhotep, Hapi (‘neck’), or small lobe region. We want to emphasize that we use these naming schemes only for convenience in descriptions/discussions, since they are now generally accepted and understood by the community. Nevertheless, ¹http://www.meshlab.net/
Fig. 1. Temperature and water production rates for each facet is shown in identified geomorphological units in an exact manner (Rezac et al. 2015). It is generally not possible to disentangle contribution from the context, and Imhotep refers to the area at the bottom of the large lobe. For example, Hapi is means to be the ‘neck’ region in broader context, and they are mean to represent in any case only a broad context region. Hence, there is a need for fast evaluations of the coma model. It may require testing of several tens of full 3D coma models for each point during the MIRO mapping observations.

Table 1. Log of selected pre-rendezvous MIRO mapping observations.

| Number | Date\(^a\) (UTC) | Flag\(^b\) | \(N\) | Integration\(^d\) (min) | \((r_0)\)\(^c\) (au) | \(|\Delta \phi|\) (km) | \(|\phi|\)\(^d\) (deg) |
|--------|------------------|-----------|-------|-------------------------|-----------------|-----------------|-----------------|
| 1      | 2014-07-05T02:41 | 0         | 5 x 5 | 26                      | 3.78            | 3.63 \times 10^4 | 24              |
| 2      | 2014-07-05T15:44 | 0         | 3 x 3 | 66                      | 3.78            | 3.43 \times 10^4 | 23              |
| 3      | 2014-07-12T00:33 | 1         | 3 x 3 | 38                      | 3.78            | 1.58 \times 10^4 | 23              |
| 4      | 2014-07-12T17:57 | 1         | 3 x 3 | 110                     | 3.78            | 1.50 \times 10^4 | 23              |
| 5      | 2014-07-19T04:47 | 1         | 3 x 3 | 27                      | 3.70            | 6.60 \times 10^4 | 8               |
| 6      | 2014-07-19T11:38 | 1–2       | 5 x 5 | 12                      | 3.69            | 6.40 \times 10^4 | 8               |
| 7      | 2014-07-19T18:03 | 1–2       | 6 x 5 | 10                      | 3.69            | 6.22 \times 10^4 | 7               |
| 8      | 2014-07-19T23:39 | 1–2       | 3 x 3 | 37                      | 3.69            | 6.05 \times 10^4 | 7               |
| 9      | 2014-07-27T17:32 | 2         | 7 x 7 | 5                       | 3.65            | 2.23 \times 10^3 | 1               |

Notes. \(^a\)Approximate time of mid-point observation in a format yyyy-mm-ddTTh:mm.

\(^b\)Flag = 0 we did not use this data, 1 we applied the 3D modelling in this work with success, 2 we applied the 3D modelling, however, fitting is not reliable due to other issues (such as possible pointing offsets, continuum temperature model, etc.). For maps with flag of 1–2 only subset of pointings can be fitted well in a map. Future work is required to fit these maps in a self-consistent manner using a more accurate model of geometry, coma, and continuum model.

\(^c\)Number of RA and Dec. points in the map.

\(^d\)Average heliocentric distance for the mapping observation.

\(^e\)Average on-source integration time per point.

\(^f\)Average heliocentric distance for the mapping observation.

\(^g\)/MIRO cometocentric distance, and

\(^h\)/Average phase angle.

The coma model is the most challenging part because fitting observations may require testing of several tens of full 3D coma models for each point during the MIRO mapping observations. Hence, there is a need for fast evaluations of the coma model. It should be noted that our goal in this work is not to develop a first principles physics, self-consistent coma model. The aim is to have a coma model reflecting the main characteristics consistent with the comet shape, illumination, and orientation of the nucleus that at the end fit the MIRO line shapes. The complex, self-consistent models are yet to be developed guided by the knowledge gained from the simpler ones, such as the one presented here.

We adopt a water density model driven purely by insolation impinging on the facets of the digital shape as used in Keller et al. (2015) (model A) (see Fig. 1). A constant production rate of \(1 \times 10^{12} \text{ m}^{-2} \text{s}^{-1}\) is assumed for the night side (unilluminated facets), but otherwise the day and night side coma follows the same calculations determining the radial water density profile. It is also important to note that in the methodology and sensitivity analysis sections (Sections 3.3, 3.4, and 4), we scale down the production rate of each illuminated facet by a factor of 26 in order to have the total surface production rate at a magnitude of about \(1 \times 10^{26} \text{ s}^{-1}\). In Section 5, the production rates are scaled differently in order to match actual MIRO measurements, as will be discussed later.

For the coma grid, we use a logarithmic scale to sample spheres centred at 67P’s body centre with different radii ranging from 0.45 to 700 km. On each sphere we select 100 \(\sqrt{3} \times 100 = 10000\) points in spherical coordinates and remove those inside the shape of the nucleus.

As Fig. 2 illustrates the number density \(n(z)\) at grid point located at distance \(z\) from the facet fulfils the following formula:

\[
Q_1 \, dr = S_{\text{sphere}}(z) n(z) V_{\exp}(z) \, dz, \tag{1}
\]

where \(Q_1 = S \times Z\) and \(S\) and \(Z\) are facet area and production rate (molecules m\(^{-2}\) s\(^{-1}\)) respectively. \(S_{\text{sphere}}(z)\) is the area of the cross-section of the sphere in the cone at surface distance \(z\). The opening angle \(\theta\) is employed to describe the solid angle \(\Omega\) of the surface outgassing with the relationship \(\Omega = 2 \pi (1 - \cos \theta)\). Then we have

\[
S_{\text{sphere}}(z) = \Omega R^2 = 2 \pi (1 - \cos \theta) R^2. \tag{2}
\]

\(R\) is the radius of the reference sphere centred at \(O\), where \(O\) is the apex of the cone and could be considered as an equivalent source point with total production rate of \(Q_1\), as shown in Fig. 2. Suppose a circle with the same area as the triangle facet has a radius of \(r\), we have the height of the cone as following:

\[
R_c = \left| O O' \right| = \frac{\sqrt{3} \pi}{\tan \theta}. \tag{3}
\]
where \( O \) is the facet centre. \( \vec{O}O' \) points along the direction of the facet’s normal vector. For an arbitrary grid point \( P \) in the coma model, we have

\[
R = |\vec{O}P|, \tag{4}
\]

surface distance \( z \) of a grid point \( P \) is defined as the distance between \( P \) and the intersection of \( \vec{O}P \) with the facet, as shown in Fig. 2.

Substitute (4) into (2) and then (2) into (1), taking the finite lifetime against photodissociation into consideration, we arrive to an expression to determine number density at surface distance \( z \):

\[
n = \frac{Q_f}{2\pi R^2(1 - \cos \theta) V_{\text{exp}}} \times e^{-\left(10^{-5}/r_h\right)^2 \times \frac{\pi}{r_h^2}}, \tag{5}
\]

where \( 10^{-5} \, \text{s}^{-1} \) is the inverse of lifetime of water molecules against photodissociation at 1 \( \text{au} \) scaled by appropriate heliocentric distance, \( r_h \).

When \( \theta = 180^\circ \), a purely spherical (Haseer model) is presented (but non-physical for an individual facet). For \( \theta = 90^\circ \), the hemispherical Haser limit is recovered above a given facet.

In addition, we consider the effects of a given facet’s surrounding morphology. For this bi-lobed nucleus, Hapi is a special region showing a highly concave structure (right-hand panel in Fig. 2). The cliffs from two lobes prevent some molecules from escaping such that the coma produced by Hapi is diluted (due to an assumption of an absorbing boundary). This ‘shadowing’ effect is accounted for during test for the visibility of the facets from any given coma sampling point.

The temperature \( T \) and velocity \( V_{\text{exp}} \) are based on the analytical formulations used with reasonable success in the 1D analysis of MIRO measurement in Gulkis et al. (2015), Lee et al. (2015), and Biver et al. (2015). Explicitly, at a given surface distance \( z \):

\[
V_{\text{exp}} = \tan(h(z/2400 \, \text{m})) \times v_m, \tag{6}
\]

the direction of velocity is considered to be along the vector of \( \vec{O}O'P \). The \( v_m \) parameter is the terminal velocity, and its maximum value noted in equation (7) is evaluated by looking at typical values of Doppler shift in MIRO lines in 2014 July. For the early observation case, \( v_m \) has the following values:

\[
v_m = \begin{cases} 
750 \, \text{m s}^{-1} & T_f > 250 \, \text{K} \\
750 - 2.5 \times (250 - T_f) \, \text{m s}^{-1} & T_f \leq 250 \, \text{K}
\end{cases}, \tag{7}
\]

where \( T_f \) is equilibrium surface temperature and calculated with model A in Keller et al. (2015). The temperature of the coma at surface distance \( z \) is determined by

\[
T = 30.0 - 2.5 \times (30.0 - T_f) \left(\frac{1}{z}\right)^{0.3}.
\tag{8}
\]

Since similar temperature and velocity parametrization have been used in 1D models of Gulkis et al. (2015) and Biver et al. (2015), they are sufficient for our purposes as well. The main parameters, \( T_f \) and \( v_m \), are at the end estimated from the MIRO line width and line shift, in order to give reasonable LOS coma profiles (discussed in Section 5). It turns out that for these MIRO unresolved nucleus data, even a properly chosen constant profile would be sufficient for our goals from these early observations.

For any given coma sampling point we evaluate the water density by adding up the contribution of all visible facets. The resultant temperature and velocity for a given coma grid point are computed as a weighted average from all visible facets, where weights are given by the water density arriving from the different surface facets.

### 3.3 Coma model validation

In our nominal coma model, we use an opening angle of 60° (see comparisons and discussion on different opening angles in appendix Fig. A1). First, we compare our coma model water density distribution to a 3D DSMC simulation Marschall et al. (2016) in Fig. 3 for heliocentric distance of 3.74 au \((Q[\text{H}_2\text{O}] \sim 10^{26} \, \text{s}^{-1})\). The images show slices centred at 67P’s centre with normal directions along x-axis pointing to the viewer. In this qualitative comparison we find that the general coma structure is well reproduced with \( \theta = 60^\circ \). Notably, we also see that the terminator location along a given line of sight (randomly selected in the bottom right panel)
is properly captured by the model. This gives us confidence that the shape and illumination of facets are properly implemented. The difference in absolute number density in Fig. 3 is not much of a concern as the production rate will be at the end scaled to match the MIRO line shapes.

In the second step to validate the coma model, we investigated how well it can capture the diurnal variations due to nucleus rotation. For this we used the published ROSINA/COPS time-series data, as shown in Fig. 4. This figure shows the water density variations over a four day period obtained by the ROSINA COPS data (magenta circles) from Bieler et al. (2015), and the simulated water density variations for the same conditions using our nominal coma model. The different model curves correspond to different opening angles for which the coma density at the location of S/C is contributed from different facets according to our coma model. We investigate the situation for small opening angles to see whether some of the smaller variations observed in COPS time-series can be better explained with smaller angles, which does not seem to be the case. From these figures, we conclude that our coma model using the nominal opening angle $\theta = 60^\circ$ properly captures the main effects due to 3D shape, illumination and variations due to nucleus rotation.

3.4 3D non-LTE and beam synthesis model

With the 3D distribution of $T$, $V_{\text{exp}}$, and $n$ obtained from the coma model described above, we are in position to calculate the non-LTE rotational populations of the ortho-H$_2$O. This is accomplished by the LIME package, which is a 3D molecular excitation and radiation transfer code for far-infrared and (sub-)millimetre wavelengths (Brinch & Hogerheijde 2010). We use the stable version 1.7, modified to include the nucleus shape model as the lower boundary condition. The code is capable of handling multiple collision partners (water–water and water–electrons), and solar absorption effects in line excitation are also included via the so-called $g$ factors.

In this work we use the same ortho-H$_2$O non-LTE model with seven levels and nine transitions as used in previous work (Gulkis et al. 2015; Lee et al. 2015). In our nominal model, following the formalism as in Lee et al. (2011), the water–electron collisional excitation may also play a role at larger distance from the nucleus. Nevertheless, the measurements of electron density around 67P during an early activity (2014 July–August) (Edberg et al. 2015) is too low to strongly influence the simulated line amplitudes.

Once the LIME code outputs populations, we can calculate beam averaged radiance for the precise MIRO pointing as derived from the SPICE kernels for a given time. Unless otherwise specified the time is the middle of the integration duration for a specific pointing. The beam synthesis calculations assume a Gaussian shape sampled such that the projected geometrical step between rings of a constant response is about 200 m (at the comet distance). Each ring is sampled with up to 200 points (depending on the angular distance from the centre of the beam), and for each point a pencil beam radiance is calculated. The total radiance is accumulated as an averaged beam radiance for the solid angle of each point and the appropriate Gaussian response.

In order to validate accuracy of the 3D populations distribution obtained by LIME, as well as our beam synthesis code we compare them in the limit of spherical symmetry to 1D calculations, used for previous MIRO analysis (Marshall et al. 2017). The presented calculations are done for a total production rate of $10^{26}$ molecules s$^{-1}$, with constant temperature of 70 K and expansion velocity of 500 m s$^{-1}$. We choose a little higher production rate to demonstrate the opacity effects in the spectral line formation, both for non-LTE calculations and beam averaged radiances. Both the 1D and 3D calculations include full radiative transfer to take into account the effect of optical depth in deriving the mean intensity in the non-LTE. We also note that the purely spherical 3D calculation is done without including the nucleus shape, instead a sphere of 2 km radius is assumed for consistency. First, in Fig. 5 we show the relative populations of the ground state level, $1_{01}$, where the largest fraction of molecules resides. The red thin solid line and blue circles compare 1D and 3D results, for a case excluding the excitation by electrons. The solid black line and orange circles compare 1D versus
3D when the electron collisions are included in the simulation (the maximum electron temperature was set to 2000 K). In summary, the 1D and 3D non-LTE populations show excellent agreement, even for multiple-collisional partners, although, in real application the electron excitation will be neglected due to their small density during the early phase.

Next we compare the beam averaged spectra derived from the 1D and 3D populations discussed above, as shown in Fig. 6. The geometry is such that MIRO is pointing at the centre of the ‘comet’ from a distance of 15 000 km (typical distance of early observations). The comparison is very encouraging showing difference of less than 1.5 K in the positive and negative peaks of the line, as well as in the self-absorbed core of the line around $-0.5 \text{ km s}^{-1}$. The largest discrepancy appears in the line segment with a strong gradient at around $-0.1 \text{ km s}^{-1}$. This difference is most likely governed by the nature of the 3D beam synthesis rather than due to differences in the populations. The difficulty arises in sampling the 3D grid when generating the LOS pencil beams and projecting the velocity along the ray.

4 NUMERICAL STUDY OF REGIONAL OUTGASSING

Having validated the 3D non-LTE transfer and line synthesis code, we are now in the position to investigate sensitivity of unresolved MIRO measurements to different distributions of water activity on the surface. The aim of this section is to visualize how the MIRO line shapes differ when various surface areas are active. Although, these simulations are not yet designed to provide perfect match to the measurements (only the sensitivity), we do use a real MIRO geometry and pointing relevant for later applications.

4.1 Effects of regional activity

First, we set out to investigate how much difference in the MIRO line shapes can we expect for different observing geometries when taking into consideration activity only from distinct nucleus regions, namely Hapi (neck), Imhotep (El-Maarry et al. 2015), and also

the entire illuminated surface. To simulate the regional activity, relevant facets of a given region have their nominal production rates (determined by given illumination conditions) amplified by a factor of 3, while the production rate in all other regions is set to $1 \times 10^{12} \text{ m}^{-2} \text{s}^{-1}$. The structure of the near nucleus coma is shown in detail for the three cases (Hapi, Imhotep, and illumination) in Fig. 7 from the point of view of column density, along with the simulated MIRO lines (bottom right panel) from a distance of 15 000 km. The MIRO beam pointing is the same for all the shown cases, but it is not centred at the image centre, but offset by about 20 km from the nucleus, as derived from SPICE kernels.

The coma shown in Fig. 7 indicates clear differences in the structure for the different models. The activity of the entire illuminated surface yields a very homogeneous inner coma from the point of view of column density, while the activity from only the Imhotep region results in a strong heterogeneous distribution, with large high/low contrast. The Hapi only activity, as expected, shows a narrow fan-like activity, with a large fraction of the coma with low density. The differences in the outgassing pattern give rise to a different distribution of number density (and projected velocity) along the MIRO LOS, resulting in strongly different line shapes. The line amplitudes, as well as line areas differ strongly (as the number densities are different), but also the line shapes (contrast red and blue curves).

4.2 Effects of illumination/rotation

Next, we will illustrate how effects of nucleus rotation and different observing geometries also produce detectable changes in the spectral line shapes. Each of the four panels in Fig. 8 corresponds to a different time of MIRO pointing during 2014 July 12, and hence to different rotation phases of the nucleus. The panels show a water
column density as colour images covering a domain of more than 60 km, with the MIRO beam superimposed as the red circle to give visual context of the overall coma structure. The comet shape is also plotted for reference, but it is again enlarged by factor 5 to be visible. The coma model in this example assumes that only the Imhotep region is active (facets in the Imhotep region are scaled up by a factor of 3 relative to the nominal illuminated model for which the total production rate is $Q \sim 1 \times 10^{26} \, \text{s}^{-1}$, while in the other regions the production rate is set to be $1 \times 10^{22} \, \text{m}^{-2} \, \text{s}^{-1}$), in which case the simulated MIRO lines would look like as shown in Fig. 9. The simulations in Figs 8 and 9 convey a clear message that if a particular region, as distinct as Imhotep (same is true for the Hapi region) are active, we would expect to see a rather strong variations in the spectral line shapes during the mapping observations by the MIRO instrument.

4.3 Effects of observational geometry

In the following comparison, we contrast the MIRO line shapes for two different pointing geometries (hence also different illumination), for the three coma models already discussed (Hapi, Imhotep, and nominal illumination), however, we also add the 1D spherical model results. The MIRO spectra are also shown as the black noisy line in Figs 10 and 11 for reference. At this point, we are still not aiming to match the MIRO line amplitudes, instead we contrast the different line shapes from the different models (and the MIRO measurement).

We note that the 1D simulation does not depend on illumination conditions, only the radial offset from nucleus plays a role. Because of this, the 1D synthetic spectral line code is made to take into account only a half of the LOS (closer to the observer) to implicitly...
introduce a ‘night side’. This issue was already noted in the early investigation (Gulkis et al. 2015), and the same approach was taken in order to match the measured line widths, which indicate a strong day/night density dichotomy. We note that in these figures we are not trying to reproduce measured line amplitudes (which is done in the following section). Therefore, we still rely on our nominal models as discussed so far, and the focus is placed on understanding how the outgassing from different source regions produces variations in the line shapes, and how they differ from the measured ones (shown in the figures). The aim is to get a qualitative insight whether the MIRO measurements (particular line shape) can be a combination of several regional outgassing regions, or rather if we can deduce their relative contribution in the process of line formation. This reflects not only in water density, but in other parameters, such as temperature or expansion velocity should be adjusted. The comparisons are shown in Figs 10 and 11.

In both figures, we could see that the 1D calculations provide very weak match to the measured line shape in the region −0.3 to about 0.5 km s$^{-1}$, but they do provide the self-absorbed line core at about −0.7 km s$^{-1}$ (which is pronounced in Fig. 10). The calculated line shapes corresponding to the entire illuminated surface outgassing (orange curves) show a better agreement of the ‘red’ wing slope, although the nominal model density would produce slightly large line widths. The ‘Hapi only’ case of outgassing shows a small deviation from the full illumination line shape, but it does reproduce both, the ‘red’ and ‘blue’ portion of the line shape very well. Finally, the ‘Imhotep’ region, which happens to be oriented away from the observer such that we see very little water number density in the beam. Overall, these results suggests that a combination of illumination and enhanced activity in the Hapi region may produce the correct line shape and amplitude.

The second geometry, Fig. 11, yields a smaller measured line amplitude as the pointing is further away from the nucleus (Fig. B1), and as a result the line core is also only weakly self-absorbed (but still clearly blue shifted). In this geometry, the nominal illumination case shows a rather weak match to the measured line shape. On the other hand, the ‘Hapi’ only outgassing in this nucleus orientation does a good job reproducing the blue and red wings slopes as well as the red wing line amplitude, but the line width in this case is little too narrow near the base of the spectral line. Therefore, just as pointed out previously, combining the illumination and Hapi activity can perhaps yield a better fitting of the measured line shapes, which is the approach we take in the next section.

5 APPLICATION TO MIRO MEASUREMENTS

Finally, after understanding the line shape sensitivity we are in the position of trying to match the observed line amplitudes and line shape for all the points in the MIRO map performed in 2014 July. As indicated in Table 1, we do not analyse the first two events in the context of this paper as they are too noisy (flag $= 0$ in the table). Events analysed with reasonable success are indicated with flag $= 1$, and we discuss them in detail in this section.

First, we analyse the map from 2014 July 11. In order to match the line amplitude and line shape, we made the following adjustments to the production rates. At each illuminated facet, we scale the production rate by 0.1, but the Hapi region is scaled only by 0.5. In previous section we used ‘Hapi only’ which was scaled up by factor 3 [which we will call (Hapi$^3$)], while in this section we use Hapi only region scale as 0.5 x 3, which we refer to as (Hapi$^+$). We make this distinction only for reader to have a connection to the sensitivity studies shown previously.

In Fig. 12, we show the full map performed on 2014 July 12, individual map points are numbered (1–9) and respective pointing geometries are shown as an offset from the nucleus centre in (km). The measurements are plotted in black. The largest amplitude is for map point 6 of about 22 K and the smallest amplitude of approximately 9 K for geometry number 3 and 9. When we compare the simulated Hapi$^3$ (blue) and Hapi$^+$ (red) spectra with the observations, we find generally a good agreement in the line shapes, for both the red and the blue wings. In fact, the red wings show an excellent fit with observations, exhibiting the correct slopes at the base and core of the lines, which means that the day–night transitions in the coma are captured reasonably well by the model. Nevertheless, the self-absorbed blue wings in the simulated spectra are overestimated (deeper) than in measurements, more importantly so for the far away pointings (e.g. map points 2, 3, and 9). From the physics of line formation, this would point in the direction of an improper gradient of expansion velocity projected along the MIRO LOS, and perhaps a larger water density as well. In our tests, we were able to modify the coma at individual point to provide a better fit in the blue wing, however, no single correction worked well for all the points in the map.

Furthermore, the line amplitudes could not be matched precisely for all points in the map with either of the models. The Hapi$^+$ is marginally better in agreement with the measured spectra amplitude and also the line width to some degree. However, the fact that calculated line amplitudes at the third pointing is greater than the first is puzzling as it contradicts the measurements. A similar problem appears for points 4 and 6, where calculations do not agree with measurements. From the model point of view, we have checked that the coma generated for time stamps corresponding to the start, middle, or end of the on-source integration do not yield a large difference in line amplitudes. Secondly, we have rechecked that the
pointing stability for the entire integration for a given point (during which four instrument calibrations occurred) scatter within about 1–2 arcsec, which is small compared to 412 arcsec or the beamwidth. Therefore, at this point we cannot adjust the pointing in a way that could improve the fit for this set of observations.

Fig. 13 shows another mapping observation we investigated in detail, 2014 July 19. It is also a 3-by-3 mapping campaign but the comet-spacecraft distance was about half compared to that of 2014 July 12.

In this case the entire map can be modelled consistently, without having the unresolved issues observed in 2014 July 12 where the amplitudes did not match observations. For 2014 July 19 the model correctly predicts the line amplitude variations for different geometries, and it is clearly visible that the Hapi+ model provides a better overall agreement with the observations. We can also conclude that the line width at the base, the red wing slope, and the line shape itself carry an information that can be used to estimate which nucleus regions contribute to the total number density inside the MIRO beam. We derive the following conclusions from our numerical study of regional sensitivity and fitting the MIRO measurements:

(i) We demonstrated that accounting for the 3D shape model, proper orientation, illumination, and viewing geometry, the line shapes may deviate strongly from the 1D spherical approximation. Although this fact is not surprising, it is important to demonstrate the limits of 1D modelling already at distances where the beam size is several times the nucleus diameter. We would expect this deviation to be even stronger for near nucleus observations.

(ii) The MIRO line shapes show a strong dependence on water activity originating at different nucleus regions. In this connection, we found that the Imhotep outgassing, even if producing enough water molecules, would not be able to match the MIRO spectral line shapes. We conclude that the Imhotep region contributes a
negligible fraction of the total number of water molecules into the MIRO beam due to direct surface outgassing. This is also true for a potential distributed water source in the coma originating from Imhotep under the assumption that the icy particles follow a radial expansion.

(iii) We investigated effects of nucleus rotation on the MIRO line shapes considering activity only from the Imhotep, Hapi and also the entire illuminated surface. In these simulations, the variations of the line shape and the line amplitude due to changing insolation as the nucleus rotates are detectable. This is additional evidence that MIRO measurements can constrain regional activity in a qualitative and, to a degree, in a quantitative way.

(iv) Fitting the MIRO measurements with a single 3D coma model (accounting only for changing illumination due to rotation) for all the map points for 2014 July 12 and July 19, we conclude that the Hapi (‘neck’) region is indeed the strongest contributor. However, other parts of the nucleus must be active as well in order to provide a good fit to the line widths and amplitudes. We found a reasonable match to observations for scaling the illumination driven outgassing in other regions by factor 0.1 except the Hapi region, which is scaled up by 1.5 from its nominal illumination value. We also find that there must exist a very strong day/night dichotomy in the water density in the coma during this onset of activity, suggesting only a very little day/night transport of water around the nucleus.

(v) Although regional outgassing sensitivity was the main focus of this work, we can also estimate the average total production rate for each map using this model. We evaluate the $Q[\text{H}_2\text{O}]$ to be $(2.5 \pm 1) \times 10^{25} \text{ s}^{-1}$ for 2014 July 12, and $(1.8 \pm 0.3) \times 10^{25} \text{ s}^{-1}$ for 2014 July 19. The standard deviation represents a scatter of values for different pointing geometries. The uncertainty in total $Q[\text{H}_2\text{O}]$ is estimated to be approximately a factor 2 due to uncertainties in coma temperatures, to smaller degree due to electron density (and temperature) and spectral calibration. The spectroscopic and collisional parameters do not play a strong role by themselves during this period. The derived $Q[\text{H}_2\text{O}]$ agree with the early evaluations of this work, we can also estimate the average total production rate for the entire illuminated surface. In these simulations, the variations of the line shape and the line amplitude due to changing insolation as the nucleus rotates are detectable. This is additional evidence that MIRO measurements can constrain regional activity in a qualitative and, to a degree, in a quantitative way.

(vi) The case for constraining the regional nucleus activity is even stronger for later observations as the spacecraft gets closer to the comet and the projected MIRO beam becomes smaller. Nevertheless, we find the nominal illumination driven outgassing, simple equilibrium surface temperature, and perhaps even pointing errors in the provided SPICE kernels contribute to the fact that we cannot match the line shapes, the line continua, and ultimately the line amplitudes in any reasonable way. Therefore, these observations should be revisited with more physical models, including proper thermal model of the sub-surface.

(vii) Finally, we also note that there is a need for a rather ‘sharp’ coma terminator to fit the MIRO line shapes in 2014 July. We have achieved this effect by using an opening angle of outgassing for each facet. It is not yet obvious that 3D DSMC codes will be able to reproduce this effect, but it should be investigated in the future.

This work constitutes the first attempt to look at the MIRO data using 3D coma, non-LTE radiative transfer model and beam synthesis codes, accounting for the nucleus shape. The Rosetta/MIRO data provide an excellent opportunity to start building and testing physical models of heat and mass transport from subsurface and the relationship to the kinetics in the coma. We provide first validation that 1D spherical models can be adequately used during this early period for total water production rate estimations (matching line area). However, reproducing the measured line shapes carried additional information which cannot be captured properly with 1D models. The 3D models of the coma can test regional or geomorphological units for activity, and they may include more complex physics of gas flow, or test dust/gas interaction. We do not suggest that MIRO spectra alone cannot uniquely constrain all these parameters, however, we believe that multi-instrument self-consistent modeling should be the way into the future analysis of Rosetta data. Only in this way, we may hope to test validity of the current models of physics of activity and plan for the future observations.

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APPENDIX A: THE USAGE OF OPENING ANGLE

Several tests have been performed varying the opening angle, \( \theta \), as defined in Section 3.2. It was found that using \( \theta = 90^\circ \) (pure hemispheric outgassing from each facet) produces a strongly homogeneous coma, but more importantly the simulated MIRO line shapes implied too many molecules around the terminator. Therefore, we settled to use \( \theta = 60^\circ \) in our nominal models, which kept the dayside coma structure, but provided a better defined terminator effect, as contrasted in Fig. A1 below. It should be understood that \( \theta = 60^\circ \) is not a precise required value. There is an entire range of opening angles (55–75\(^\circ\)) which would provide the same conclusions within other uncertainties of the modeling, and the MIRO measurement uncertainties.

![Figure A1. Comparison of the water density (m\(^{-3}\)) calculated from our coma model for two opening angle: \( \theta = 60^\circ \) for the left two panels and \( \theta = 90^\circ \) at the right-hand side. The scale of the coma is about 60 km in the upper two panels and about 20 km in the bottom ones. A suitable 3D structure around terminator could not be produced properly when OPA = 90\(^\circ\) as shown in the right-hand panels. The plots show slices when looking into the +Y direction in CG’s body frame.](https://example.com/fig1.png)

APPENDIX B: MIRO MAPPING OBSERVATION 2014 JULY 12

It is very challenging to contain all the necessary information for the interpretation of MIRO observations in a single figure. Especially the mapping observations of MIRO are difficult to visualize with respect to the offset from the comet centre, the beam size, the illumination condition of the nucleus, coma temperature, density, expansion velocity, and other parameters. In the main text, when discussing an isolated effect of a coma or nucleus on the MIRO line shape, we limit the information only to the relevant parameter in question, neglecting others for clarity. Therefore, here we would like to provide, in addition, an overall context of the 3x3 mapping observation in 2014 July 12 (Fig. B1), which is used in this study.

![Figure B1. A plot of the MIRO geometry and line areas for the 2014 July 12 map. The x- and y-axis show the pointing distance (km) of MIRO relative to the comet centre projected on to the viewing plane using the SPICE library. The comet centre is at (0, 0) on the plot. The average pointing during an integration at a specific point is marked with a red cross, an outline of the beam (FWHM) is plotted as black larger circles, and the colour filled circles contains information about the integrated line area (K km s\(^{-1}\)) (as indicated in the colourbar). The size of the colour filled circle is arbitrary, and set only for good visual clarity. The numbers associated with each point in the map give a clue about the order the observations were made, and we also refer to them in the main text when discussion a particular pointing geometry, e.g. map point number 1, 2, etc.](https://example.com/fig2.png)